# New Extended Clusters in Ternary Molybdenum Oxides* 

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#### Abstract

Three new compounds representative of different structure types in the family of ternary metal oxides with extended metal-metal bonded arrays are discussed. $\mathrm{InMO}_{4} \mathrm{O}_{6}$ (isomorphous with $\mathrm{NaMo}_{4} \mathrm{O}_{6}$ ) contains infinite anion chains of condensed octahedral cluster units, $\left(\mathrm{Mo}_{4} \mathrm{O}_{6}^{-}\right)_{\infty}$, crosslinked to form channels where $\mathrm{In}^{+}$cations reside in sites of square pyramidal coordination to oxygen. The linear array of In atoms in the channels, with $d(\mathrm{In}-\mathrm{In})=2.8628(4) \AA$, suggests some degree of $\mathrm{In}-\mathrm{In}$ bonding, and these interactions may contribute to the metallic conductivity determined for this compound over the range $2-300 \mathrm{~K}$. Infinite chains with $\mathrm{Mo}_{2} \mathrm{O}_{4}$ repeat units condensed as rhomboidal clusters fused on opposite edges are the outstanding structural feature of $\mathrm{NaMo}_{2} \mathrm{O}_{4}$. The compound also has a doublelayer lattice $\mathrm{MoO}_{2}$ with $\mathrm{Na}^{+}$ions fractionally occupying octahedral coordination sites between alternate layers. The compound $\mathrm{Ca}_{5.45} \mathrm{Mo}_{18} \mathrm{O}_{32}$ contains three different kinds of cluster chains with $\mathrm{Mo}_{1}$, $\mathbf{M o}_{2}$, and $\mathbf{M o}_{4}$ repeat units. Metal cluster electron counts on the three different repeat units, estimated from $\mathrm{Mo}-\mathrm{O}$ bond strength-bond distance relations, are reflected in the formula $\mathrm{Ca}_{5.45}\left(\mathrm{MoO}_{3}^{2.26-}\right)_{2}\left(\mathrm{Mo}_{2}\right.$ $\left.\mathrm{O}_{3.5}^{0.22-}\right)_{4}\left(\mathrm{MO}_{4} \mathrm{O}_{6}^{2.65-}\right)_{2}$.


## Introduction

Until recently metal oxide phases with readily apparent extended arrays of metalmetal bonded units were relatively rare. The $\beta$-modification of $\mathrm{ReO}_{2}$ (1), NbO (2), and the platinum bronze phases (3) which contain linear chains of weakly metalmetal bonded, square planar coordinated platinum atoms, were essentially the only

[^0]structurally well-characterized examples. Since the dividing lines are rarely distinct one may also include in this category the early transition metal suboxides (4), where the bonding is surely dominated by metalmetal interactions similar to those in the pure elements. The dioxides with the undistorted rutile structure (5), viz. $\mathrm{TaO}_{2}, \mathrm{RuO}_{2}$, $\mathrm{OsO}_{2}, \mathrm{RhO}_{2}$, and $\mathrm{IrO}_{2}$, though possessing metallic character, may be excluded from this category because their structures are dictated largely by the metal-oxygen bonding, and the metal-metal interactions at distances of $>3.0 \AA$ are much weaker. In the interesting case of $\mathrm{LiNbO}_{2}$ (6) the conclusions about metal-metal bonding are uncertain. This structure is like that of $2 \mathrm{H}-\mathrm{MoS}_{2}$ with Li intercalated into the van der Waals gap. The $\mathrm{Nb}-\mathrm{Nb}$ distance of $2.90 \AA$ within
the hexagonal close-packed layers of Nb atoms are obviously short enough for a strong contribution from $\mathrm{Nb}-\mathrm{Nb}$ bonding, but here it is not clear whether this is sufficient to dictate the structure.

The discovery of $\mathrm{NaMo}_{4} \mathrm{O}_{6}$ (7) greatly expanded our vision of new chemistry which might be possible in metal-metal bonded oxide systems. This structure, consisting of $\mathrm{Mo}_{6} \mathrm{O}_{12}$-type octahedral cluster units condensed by fusion on opposite edges to form infinite anion chains [ $\left(\mathrm{Mo}_{2}\right.$ $\left.\left.\mathrm{Mo}_{4 / 2} \mathrm{O}_{8 / 2}^{i} \mathrm{O}_{2 / 2}^{i-a} \mathrm{O}_{2 / 2}^{a-i}\right)^{-}\right]_{\infty}$ was unprecedented among those known for oxide compounds. However, related structures were found somewhat earlier for $\mathrm{Sc}_{5} \mathrm{Cl}_{8}(8)$ and reduced halides of the lanthanide elements (9). We thus initiated a synthetic program to explore the structures that might exist in this new realm. Only new compounds with extended metal-metal bonded arrays (infinite chains) will be included in this discussion.

## Synthesis

Among the compounds discussed here not all have been produced in single phase form. In general the composition of each new compound has been established through a combination of electron microprobe analysis and X-ray structure refinement of single crystals selected from reaction mixtures. Once the composition was established reactions were attempted for synthesis of the pure compound in polycrystalline form from stoichiometric mixtures of metal and metal oxide in pressed pellets. According to Guinier X-ray powder patterns single phase reaction products have been obtained in the following cases:
(i) $3 \mathrm{Na}_{2} \mathrm{MoO}_{4}+8 \mathrm{MoO}_{3}+13 \mathrm{Mo} \rightarrow$

$$
6 \mathrm{NaMo}_{4} \mathrm{O}_{6}
$$

(pressed pellet in sealed Mo tube, $1100^{\circ} \mathrm{C}, 5 d$ )
(ii) $\mathrm{In}+2 \mathrm{MoO}_{3}+2 \mathrm{Mo} \rightarrow \mathrm{InMo}_{4} \mathrm{O}_{6}$ (pressed pellet in sealed fused silica tube, $895^{\circ} \mathrm{C}, 28 d$ )
(iii) $9 \mathrm{Sc}_{2} \mathrm{O}_{3}+30 \mathrm{ZnO}+37 \mathrm{MoO}_{3}$

$$
+59 \mathrm{Mo} \rightarrow 24 \mathrm{Sc}_{0.75} \mathrm{Zn}_{1.25} \mathrm{Mo}_{4} \mathrm{O}_{7}
$$

(pressed pellet in sealed Mo tube, $1450^{\circ} \mathrm{C}, 7 d$ )
(iv) $5.45 \mathrm{CaMoO}_{4}+3.40 \mathrm{MoO}_{3}$

$$
+9.15 \mathrm{Mo} \rightarrow \mathrm{Ca}_{5.45} \mathrm{Mo}_{18} \mathrm{O}_{32}
$$

(pressed pellet in sealed Mo tube, $1435^{\circ} \mathrm{C}, 3 d$ ).

In the case of $\mathrm{NaMo}_{2} \mathrm{O}_{4}$ pure single phase material has not yet been prepared. Single crystals, in the form of thin platelets, were selected from a reaction conducted under the following conditions.:
(v) $1.64 \mathrm{Na}_{2} \mathrm{MoO}_{4}+2.3 \mathrm{MoO}_{2}$
$+\mathrm{Mo} \rightarrow \mathrm{NaMo}_{2} \mathrm{O}_{4}+$ other products
(loose powder, sealed Ni tube, $900^{\circ} \mathrm{C}$, $3 d$ ).

## Structure Types

A complete listing of the structure types that have been elucidated in detail is given in Table I. All of these structures are characterized by infinite Mo-Mo bonded chains consisting of either $\mathrm{Mo}_{4}$ or $\mathrm{Mo}_{2}$ repeat units. The chains having $\mathrm{Mo}_{4}$ repeat units may be considered as condensed octahedral cluster units sharing opposite edges, derived from the $\mathrm{Mo}_{6} \mathrm{O}_{12}$ discrete cluster type by elimination of the two O atoms on the edges to be shared (14). Sharing of O atoms between repeat units leads to the connective formula $\mathrm{Mo}_{2} \mathrm{Mo}_{4 / 2} \mathrm{O}_{2} \mathrm{O}_{8 / 2}$. Crosslinking of these chains through Mo-O-Mo bridge bonding in different ways then provides the framework and coordination sites for the ternary metal cations in the various structure types, I-IV. The chains having $\mathrm{Mo}_{2}$ repeat units conceptually are derived by condensation of rhomboidal clusters $\mathrm{Mo}_{4} \mathrm{O}_{16}$ by sharing metal at-

TABLE I
Structure Types for Compounds Having Infinite Chain Structures among Reduced Molybdenum Oxide Phases

|  | Structure type | Crystal class | Lattice constants | Space group | Isomorphous members | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | $\mathrm{NaMo}_{4} \mathrm{O}_{6}$ | Tetragonal | $a=9.570(3)$ | P4/mbm | $M_{M 04} \mathrm{O}_{6}(\boldsymbol{M}=\mathbf{K}, \mathrm{Rb}, \mathrm{In})$ | 8 |
|  |  |  | $c=2.8634(8)$ |  | $\mathrm{Sn}_{0.9} \mathrm{Mo}_{4} \mathrm{O}_{6}$ | 11 |
| II | $\mathrm{Ba}_{5}\left(\mathrm{Mo}_{4} \mathrm{O}_{6}\right)_{8}$ | Orthorhombic | $\begin{aligned} a & =9.517(1) \\ b & =9.822(1) \end{aligned}$ | Pbam | $\mathrm{Sr}_{\mathrm{x}} \mathrm{MO}_{4} \mathrm{O}_{6}$ ? | 12 |
|  |  |  | $c=22.813(4)$ |  |  |  |
| III | $\mathrm{Sc}_{0.75} \mathrm{Zn}_{1.25} \mathbf{M o}_{4} \mathrm{O}_{7}$ | Orthorhombic | $\begin{aligned} & a=6.085(1) \\ & b=17.002(4) \end{aligned}$ | Imam | $M_{x} M_{2-\mathrm{x}}^{\prime} \mathrm{Mo}_{4} \mathrm{O}_{7}\left[M, M^{\prime}=\mathrm{Ti}_{0 . S} \mathrm{Zn}_{1.5},\right.$ <br> $\mathrm{Sc}_{0.5} \mathrm{Fe}_{1.5}, \mathrm{Fe}\left(\mathrm{Fe}_{0.9} \mathrm{Mo}_{0.1}\right)$, | 13 |
|  |  |  | $c=5.764(1)$ |  | $\mathrm{Zn}\left(\mathrm{Zn}_{0.4} \mathrm{Al}_{0.5} \mathrm{Mo}_{0.1}\right)^{\text {a }}$ ] |  |
| IV | $\mathrm{Mn}_{0.7} \mathrm{Mo}_{4} \mathrm{O}_{5.5}$ | Monoclinic | $\begin{aligned} & a=9.859(3) \\ & b=16.921(4) \end{aligned}$ | $P 2_{1} / a$ | None | 14 |
|  |  |  | $\begin{aligned} & c=2.846(1) \\ & \beta=94.94(4) \end{aligned}$ |  |  |  |
| v | $\mathrm{Na}_{0.9} \mathrm{Mo}_{2} \mathrm{O}_{4}$ | Monoclinic | $\begin{aligned} & a=12.448(9) \\ & b=2.893(3) \end{aligned}$ | C2/m | None | This work |
|  |  |  | $\begin{aligned} & c=4.934(3) \\ & \beta=104.02(7) \end{aligned}$ |  |  |  |
| vI | $\mathrm{Ca}_{5.45} \mathrm{Mo}_{18} \mathrm{O}_{32}$ | Monoclinic | $a=24.234(7)$ | C2/m | None | This work |
|  |  |  | $b=2.8503(7)$ |  |  |  |
|  |  |  | $c=9.875(7)$ |  |  |  |
|  |  |  | $\beta=109.82(4)$ |  |  |  |

oms on opposite edges and O atoms between units, as indicated by the connective formula for $\mathrm{V}, \mathrm{Na}\left(\mathrm{Mo}_{4 / 2} \mathrm{O}_{2} \mathrm{O}_{8 / 2} \mathrm{O}_{6 / 3}\right)$. In this case the metal chains are included between close-packed layers of O atoms, and the $\mathrm{Na}^{+}$ions are located in partially occupied, octahedral coordination sites between alternate layers.

Structure type VI is the most complicated found so far, in that three types of infinite chains occur within the same structure. This is indicated in the formula $\mathrm{Ca}_{5.45}\left(\mathrm{MoO}_{3}\right)_{2}\left(\mathrm{Mo}_{2} \mathrm{O}_{72}\right)_{4}\left(\mathrm{Mo}_{4} \mathrm{O}_{6}\right)_{2}$ which reflects the presence of chains containing fused rhomboidal units as in $\mathbf{V}$, fused octahedral units as in I-IV, and single atom chains like those found in the M-M bonded dioxides having the distorted rutile structure, e.g., $\mathrm{MoO}_{2}$ (15). Here there is unusual difficulty in assessing the apportionment of electrons for metal-metal bonding within the three kinds of repeat units. From the formula we may assume that a total of 10.9 electrons is transferred from Ca to the molybdenum oxide chains, but in what proportion are they distributed? This aspect has
been examined and resolved within reasonable limits as discussed in a subsequent section.

Three of the compounds listed in Table I will be discussed in more detail. Each was chosen as a new compound representative of a very different structure type, as presenting unique problems in the interpretation of electron counting and bonding features, and as presenting interesting variants of important physical properties. We have thus chosen $\mathrm{InMo}_{4} \mathrm{O}_{6}$, type I, $\mathrm{NaMo}_{2} \mathrm{O}_{4}$, type V , and $\mathrm{Ca}_{5.45} \mathrm{Mo}_{18} \mathrm{O}_{32}$, type VI, for this purpose.

InMo ${ }_{4} \mathrm{O}_{6}$. This compound is isomorphous with $\mathrm{NaMo}_{4} \mathrm{O}_{6}$. A view of the structure is shown in Fig. 1, which depicts the infinite $\mathrm{Mo}_{4} \mathrm{O}_{6}$ chains running parallel to the unique axis, and position of the In atoms in the channels created by crosslinking of the chains. Both analytical data and X-ray structure refinement show that the composition is very close to stoichiometric In $\mathrm{Mo}_{4} \mathrm{O}_{6}$. The In atoms are located in sites slightly displaced ( $0.28 \AA$ ) from the plane of four equidistant O atoms, $d(\operatorname{In}-\mathrm{O})=$


Fig. 1. (A) A three-dimensional view down the $c$ axis of $\mathrm{InMo}_{4} \mathrm{O}_{6}$. (B) The $\mathrm{Mo}_{4} \mathrm{O}_{6}$ cluster chain of In $\mathrm{Mo}_{4} \mathrm{O}_{6}$ as viewed perpendicular to the chain axis. Heavy lines are Mo-Mo bonds and thin lines are MoO bonds.
$2.390(7) \AA$, each of which belongs to a separate $\mathrm{Mo}_{4} \mathrm{O}_{6}$ chain. This coordination geometry for In suggests that a sterically active lone pair of electrons projects radially away from the $\mathrm{InO}_{4}$ pyramid, and that the cation is present as $\mathbf{I n}^{+}$. Confirmation of $\operatorname{In}(1+)$ comes from the In-O bond strength sum computed from the relation of Brown and $\mathrm{Wu}(16), s(\operatorname{In}-\mathrm{O})=[d(\operatorname{In}-\mathrm{O}) / 1.959]^{-7.0}=$ $(2.390 / 1.959)^{-7.0}=0.25 ; \Sigma s=$ valence $=$ $4(0.25)=1.00$. The latter is also consistent with a formal charge of -1.15 on the $\mathrm{Mo}_{4} \mathrm{O}_{6}$ units of the anion chains, computed in a similar way from the Mo-O bond strengthbond distance relation $s(\mathrm{Mo}-\mathrm{O})=[d(\mathrm{Mo}-$ O) $/ 1.882]^{-6.0}$ (17).

In this structure linear chains are formed from the In atoms, which are spaced only $2.8628(4) \AA$ apart within the channels. W may then ask if In -In bonding is important
in these chains. A comparison of this distance with In-In distances in the metal, 3.24 and $3.37 \AA$, suggests that In-In bonding may be important. However, In-In distances in compounds where metal-metal bonding is more certain, e.g., $\mathrm{In}_{6} \mathrm{~S}_{7}$ (18), $\gamma$ InSe (19), and $\mathrm{In}_{4} \mathrm{Se}_{3}$ (20), average about $2.76 \AA$, and these usually contain In atoms in a higher formal oxidation state. We thus conclude that $\mathrm{In}-\mathrm{In}$ bonding in $\mathrm{InMo}_{4} \mathrm{O}_{6}$ is likely to be weak, but may contribute in an important way to the electrical conductivity and other physical properties. Resistivity measurements parallel to the $c$-axis on a single crystal in the range $2-300 \mathrm{~K}$ clearly demonstrate that $\mathrm{InMo}_{4} \mathrm{O}_{6}$ is metallic, with $\rho($ parallel $)=160 \times 10^{-6}$ ohm cm at 298 K .

The Mo-Mo bond distances within the $\mathrm{Mo}_{4} \mathrm{O}_{6}^{-}$anion chains of $\mathrm{InMo}_{4} \mathrm{O}_{6}$ are quite similar to those in $\mathrm{NaMo}_{4} \mathrm{O}_{6}$ (7), as expected if the compounds are indeed isoelectronic. This is also confirmed by the Mo-O bond strength sums which indicate that the anion chains in $\mathrm{NaMo}_{4} \mathrm{O}_{6}$ and $\mathrm{InMo}_{4} \mathrm{O}_{6}$ bear the same charge.
$\mathrm{NaMo}_{2} \mathrm{O}_{4}$. Essential features of this structure are shown in Figs. 2 and 3. The layer arrangement shown in Fig. 2 is similar to that in the $\mathrm{CdCl}_{2}$ or $\mathrm{CdI}_{2}$ structures, in that the metal atoms are included in octahedral sites between close-packed oxide layers. Octahedral sites between every other layer are occupied fully by Mo atoms, and these sites in the alternate layers are approximately half-occupied by Na ions. Thus the Na ions can be viewed as intercalated within the van der Waals gap of the $\mathrm{MoO}_{2}$ layer lattice. Within the $\mathrm{MoO}_{2}$ layers the Mo atoms are shifted from the center of their octahedral sites toward neighboring Mo atoms such that the infinite chains of fused rhomboidal cluster units are formed parallel to the short $b$ axis, as shown in Fig. 3. Each Mo atom thus is bonded to two Mo atoms parallel to the chain direction at 2.893(2) $\AA$, and to two other Mo via the zigzag bonds at $2.535(2) \AA$. From the for-


Fig. 2. The structure of $\mathrm{NaMo}_{2} \mathrm{O}_{4}$ as viewed down the $b$ axis. Mo-Mo bonds are indicated by multiple lines, Mo-O bonds by single lines. Na atoms shown by unconnected ellipsoids.
mula $\mathrm{NaMO}_{2} \mathrm{O}_{4}$ we conclude that each Mo atom has 2.5 electrons (average) for participation in the metal-metal bonding. If the short bonds are considered as normal electron pair bonds, each Mo must contribute one electron to each of these bonds. The remaining 0.5 electron/Mo must then enter into the long bonds in the chain direction. Each long bond should then attain bond order 0.25 , in rough agreement with the bond order, 0.34 , calculated from $d=2.893 \AA$ using the Pauling (21) relation $d$ (obs.) $=d_{1}$ $-0.6 \log n$, where $d_{1}$ is the single bond distance, $2.614 \AA$, computed from the distances in Mo metal, and $n$ is the bond order. Equal spacing of the Mo atoms along the chain direction suggests that the bonding is delocalized and that the compound should exhibit high conductivity in the $b$ direction. Interchain distances, $d(\mathrm{Mo}-\mathrm{Mo})=3.200(2)$ $\AA$, suggest that the interchain Mo-Mo in-
teractions are very weak. Similarly, interlayer interactions should be even weaker, thus conductivity in both the $a$ and $c$ directions is expected to be quite small.

The structure of $\mathrm{NaMo}_{2} \mathrm{O}_{4}$ stands in sharp contrast to that of $\mathrm{Ba}_{1.14} \mathrm{Mo}_{8} \mathrm{O}_{16}$ (22) and $\mathrm{K}_{2} \mathrm{Mo}_{8} \mathrm{O}_{16}$ (23) where similar chains of Mo atoms are broken into discrete rhomboidal cluster units. The electron/Mo ratios, 2.28 for $\mathrm{Ba}_{1.14} \mathrm{Mo}_{8} \mathrm{O}_{16}$ and 2.50 for Na $\mathrm{Mo}_{2} \mathrm{O}_{4}$, are sufficiently close that the structural difference of discrete cluster units vs extended chains is not readily understood. In fact, the $2.50 e / \mathrm{Mo}$ in Na $\mathrm{Mo}_{2} \mathrm{O}_{4}$ should be ideal for forming the $10 e$, completely bonded rhomboidal cluster unit like those found in the regular cluster units of $\mathrm{Ba}_{1.14} \mathrm{Mo}_{8} \mathrm{O}_{16}$. Experiments are in progress to explore the possible oxidation-reduction chemistry of $\mathrm{NaMo}_{2} \mathrm{O}_{4}$ according to
$\mathrm{NaMo}_{2} \mathrm{O}_{4}$

$$
\begin{equation*}
=\mathrm{Na}_{1-x} \mathrm{Mo}_{2} \mathrm{O}_{4}+x \mathrm{Na}^{+}+x e^{-} \tag{1}
\end{equation*}
$$



Fig. 3. The structure of the $\mathrm{MoO}_{2}$ layers of $\mathrm{Na}-$ $\mathrm{Mo}_{2} \mathrm{O}_{4}$ as viewed perpendicular to the layer. Multiple lines represent Mo-Mo bonds, single lines Mo-O bonds.

$$
\begin{array}{r}
\mathrm{NaMo}_{2} \mathrm{O}_{4}+\mathrm{Na}^{+}+1 e^{-} \\
=\mathrm{Na}_{1+x} \mathrm{Mo}_{2} \mathrm{O}_{4} . \tag{2}
\end{array}
$$

By such reactions it may be possible to vary the $e /$ Mo ratio in the extended chains and thereby discern if the chain construction is altered significantly as a function of this quantity. It appears that the $\mathrm{Na}^{+}$occupation within the layers, which is only $50 \%$ in Na $\mathrm{Mo}_{2} \mathrm{O}_{4}$, should be variable over the stoichiometric range $\mathrm{Na}_{2-x} \mathrm{Mo}_{2} \mathrm{O}_{4}$, with $0 \leq$ $x \leq 2$.
$\mathrm{Ca}_{5.45} \mathrm{Mo}_{18} \mathrm{O}_{32}$. A view of this structure as projected down the short axis is shown in Fig. 4. Principal features include three kinds of extended chains interconnected by Mo-O-Mo bridge bonding to provide channels in which the $\mathrm{Ca}^{2+}$ ions are located. Stoichiometrically the extended chains occur as single-atom, two-atom, and fouratom repeat units in the ratios $2 / 4 / 2$, respectively, as indicated by the anion formula units $\mathrm{MoO}_{3}^{m-}, \mathrm{Mo}_{2} \mathrm{O}_{3.5}^{n-}$, and $\mathrm{Mo}_{4} \mathrm{O}_{6}^{\prime-}$, respectively. The single-atom chains are constructed like those of the metal atom chains extended along the $c$-axis of the rutile structure, but having the metal atoms drawn together in pairs to form alternately bonded and nonbonded distances (Mo5-Mo5) of $2.560(9)$ and $3.135(9) \AA$, respectively. Thus
the metal atoms in these chains are bonded in the same fashion as those in the $\mathrm{MoO}_{2}$ (15) distorted rutile structure.

In the chains containing the two-atom repeat units the metal-metal bonding is exactly like that found in the layered compound $\mathrm{NaMo}_{2} \mathrm{O}_{4}$. The intrachain Mo-Mo distances are 2.850 (1) and 2.546(2) $\AA$, respectively, for the bonds parallel to the chain direction (Mo3-Mo3), and the zigzag bonds between atoms on parallel edges of the fused rhomboids (Mo2-Mo3). These distances compare closely with the related distances in $\mathrm{NaMo}_{2} \mathrm{O}_{4}$ and indicate the anion chains must have comparable $e /$ Mo ratios in the two compounds. This point is discussed further below.

The construction of the chains containing the four-atom repeat units is exactly like those found in $\mathrm{NaMO}_{4} \mathrm{O}_{6}$ (or $\mathrm{InMO}_{4} \mathrm{O}_{6}$ ), except that the average Mo-Mo intrachain bond distance is somewhat smaller, indicating perhaps a higher average cluster-electron count in the $\mathrm{Mo}_{4} \mathrm{O}_{b}^{p-}$ units of this compound.

For help in assessing the anion charge and metal cluster electron count on the separate chains in this complex structure we turn to the well-established empirical bond strength-bond distance relation for the


Fig. 4. The unit cell of $\mathrm{Ca}_{5.45} \mathrm{Mo}_{18} \mathrm{O}_{32}$ as projected down the $b$ axis. Positions of the various atoms in the unit cell are indicated. Mo 1 and Mo 4 belong to $\mathrm{Mo}_{4} \mathrm{O}_{6}$ units, Mo 2 and Mo 3 belong to $\mathrm{Mo}_{2} \mathrm{O}_{3.5}$ units, Mo5 to the single-atom chains.

TABLE II
Valence of Molybdenum and Net Anion Charge for Repeat Units of Chains in $\mathrm{Ca}_{5.45} \mathrm{Mo}_{18} \mathrm{O}_{32}$

| Repeat unit | Valence of Mo | Net anion charge <br> $(q-)$ |
| :--- | :---: | :---: |
| $\mathrm{MoO}_{3}$ | Mo5 3.74 | 2.26 |
| $\mathrm{Mo}_{2} \mathrm{O}_{3.5}$ | $\mathrm{Mo2} 3.42$ | 0.22 |
| $\mathrm{Mo}_{4} \mathrm{O}_{6}$ | $\mathrm{Mo3} 3.36$ |  |
|  | Mo1 2.20 | 2.65 |
|  | Mo4 2.47 |  |

Mo-O bonds ( 16,17 ). The average oxidation state or valence of each Mo atom in the structure can be obtained by summing over the bond strength $s$ for all of the Mo-O bonds attached to that atom, as given in

$$
\begin{align*}
s & =[d(\mathrm{Mo}-\mathrm{O}) / 1.882]^{-6.0}  \tag{3}\\
\Sigma s\left(\mathrm{Mo}_{\mathrm{i}}\right) & =\text { valence }\left(\mathrm{Mo}_{i}\right) . \tag{4}
\end{align*}
$$

Determination of the valence of each Mo then permits calculation of the net anion charge for each kind of repeat unit through the assumption that each O atom bears a formal charge of -2 , as given in

$$
\begin{equation*}
q=\sum_{i} n_{i} v_{i}(\mathrm{Mo})-2 n(\mathrm{O}) \tag{5}
\end{equation*}
$$

where $q$ is the formal anion charge, $n_{i}$ is the number of Mo atoms of type $i$ in the repeat unit, $v_{i}$ is the valence of Mo of type $i$, and $N(0)$ is the number of oxygen atoms in the repeat unit. The results of these calculations for the three structural units of $\mathrm{Ca}_{5.45}$ $\mathrm{Mo}_{18} \mathrm{O}_{32}$ are given in Table Il. In these computations an error of one standard deviation of the M-O bond distance results in an error of 0.01 to 0.02 in the $\mathrm{M}-\mathrm{O}$ bond strength. Since positive and negative deviations are equally likely the average error in the quantity $\Sigma s$ should also be on the order of 0.02 , but the maximum error should be ca. $\pm 0.1$ valence unit.

If the results of these calculations are
valid the sum of the anion charges per formula unit should be equal to the total cation charge from $\mathrm{Ca}^{2+}$, i.e., $2(5.45)=10.9$. We thus have for the formula $\mathrm{Ca}_{5.45}$ (Mo $\left.\mathrm{O}_{3}^{m-}\right)_{2}\left(\mathrm{Mo}_{2} \mathrm{O}_{3.5}^{n-}\right)_{4}\left(\mathrm{Mo}_{4} \mathrm{O}_{6}^{p-}\right)_{2}$ the equation

$$
\begin{align*}
\Sigma q^{-} & =2 m+4 n+2 p \\
& =2(2.26)+4(0.22) \\
& \quad+2(2.65)=10.7 \tag{6}
\end{align*}
$$

Within the expected maximum error of about $\pm 0.1$ in the charge of each anion the agreement $\Sigma q^{+}=10.9$ and $\Sigma q^{-}=10.7$ is extremely good.

A comparison of the metal cluster electron count for the three repeat units in $\mathrm{Ca}_{5.45} \mathrm{Mo}_{18} \mathrm{O}_{32}$ with those of the same units in related compounds is instructive. From $\mathrm{MoO}_{3}^{2.26-}$ we obtain $2.26 \mathrm{e} / \mathrm{Mo}$ for the MoMo bonding in the single-atom chains, which compares favorably to $2.0 \mathrm{e} / \mathrm{Mo}$ for the bonding in $\mathrm{MoO}_{2}$. That the $e / \mathrm{Mo}$ ratio is variable for structures with such singleatom chains is shown by the compound $\mathrm{LiMoO}_{2}$ (24) where the observed Mo-Mo distance, $2.46 \AA$, is somewhat shorter than that in $\mathrm{MoO}_{2}, 2.52 \AA$ (15). The charge of -0.22 on the $\mathrm{Mo}_{2} \mathrm{O}_{3.5}$ repeat unit gives a $5.22 \mathrm{e} / \mathrm{Mo}$ unit, nearly the same (probably within the margin of error) as the 5.00 $e / \mathrm{Mo}_{2}$ unit in $\mathrm{NaMo}_{2} \mathrm{O}_{4}$. As noted above the nearly equal Mo-Mo bond distances within these units in the two compounds reflect this agreement in the bonding electron count. Finally, we may compare the metal cluster electron count for the $\mathrm{Mo}_{4} \mathrm{O}_{6}$ repeat units with those in other compounds containing these units. This comparison is given in Table III where it is seen that the anion charge and MCE count of $\mathrm{Ca}_{5.45} \mathrm{Mo}_{18}$ $\mathrm{O}_{32}$ are as high as those on any of the other compounds known to contain chains with the same type of repeat unit. The structure of $\mathrm{Ca}_{5.45} \mathrm{Mo}_{18} \mathrm{O}_{32}$ is unique among these compounds in having the cation positions only partially occupied. Here the Ca positions are only $68.1 \%$ occupied, whereas the

TABLE III
Valence of Mo Atoms, Anion Net Charge, and Metal Cluster Electron Counts (MCE) for Compounds Containing Chains with $\mathrm{Mo}_{4} \mathrm{O}_{6}$ Repeat Units

| Compound | Valence ${ }^{\text {a }}$ |  | Anion charge ${ }^{a}$ ( $q^{-}$) | MCE ${ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: |
|  | Mo (waist) | Mo (apex) |  |  |
| $\mathrm{NaMO}_{4} \mathrm{O}_{6}$ | 2.46 | 3.11 | 0.85 | 12.8 |
| $\mathrm{InMo}_{4} \mathrm{O}_{6}$ | 2.46 | 2.96 | 1.15 | 13.2 |
| $\mathrm{Sc}_{0.75} \mathrm{Zn}_{1.25} \mathrm{Mo}_{4} \mathrm{O}_{7}$ | 2.04 | 2.73 | $2.46{ }^{\text {c }}$ | 14.5 |
| $\mathrm{Ti}_{0.5} \mathrm{Zn}_{1.5} \mathrm{Mo}_{4} \mathrm{O}_{7}$ | 2.08 | 2.76 | $2.33{ }^{\text {c }}$ | 14.3 |
| $\mathrm{Ca}_{5.45} \mathrm{Mo}_{18} \mathrm{O}_{32}$ | 2.20 | 2.47 | 2.65 | 14.6 |

${ }^{a}$ See text for method of determination.
${ }^{b}$ Determined from formula with anion charge of $q-$
${ }^{c}$ Anion charge based on $\mathrm{MO4}_{4} \mathrm{O}_{6}$ unit; charge will be two units greater for $\mathrm{MO}_{4} \mathrm{O}_{7}$ units.
formula for complete occupation would be $\mathrm{Ca}_{8} \mathrm{Mo}_{18} \mathrm{O}_{32}$. Why then does the compound choose the particular composition exhibited?

We find that a single crystal of $\mathrm{Ca}_{5.45} \mathrm{Mo}_{18}$ $\mathrm{O}_{32}$ is a semiconductor with a small band gap of 0.08 eV as determined from $\log \rho$ vs $T^{-1}$ over the range 30 to 298 K . Evidently at this particular composition the conduction band is filled. If we assume that all of the metal-metal bonding states within the extended chains are filled at this point, we may thereby derive an estimate of the maximum number of electrons which can populate the individual chains. This then is the significance attached to the MCE counts determined for the cluster units in this particular structure. Notably the anion charge and MCE count for the $\mathrm{Mo}_{4} \mathrm{O}_{6}$ repeat unit is highest for the calcium compound and may well represent the maximum value attainable for this kind of chain. Further work will be necessary to see if additional cations can be added to this structure to test this hypothesis.

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